

Reg. No. : .....

Name : .....

Third Semester M.Sc. Degree Examination, February 2021.

Physics

PH:231 : ADVANCED QUANTUM MECHANICS

(2014-17 Admission)

Time : 3 Hours

Max. Marks : 75

SECTION – A

Answer **any five** questions. Each question carries **3** marks.

- I. (a) What is variational principle in approximation methods?
- (b) Explain the formulation of Rayleigh Ritz trial function.
- (c) What is barrier penetration in WKB approximation method?
- (d) Prove  $[\hat{L}_x, \hat{y}] = i\hbar\hat{z}$  where  $\hat{L}_x$  angular momentum and  $\hat{y}$  and  $\hat{z}$  are position operators.
- (e) What is identity transformation?
- (f) Discuss the Pauli Exclusion principle.
- (g) Write the commutation relation between Pauli's spin matrices.
- (h) What is Lamb shift?

(5 × 3 = 15 Marks)

P.T.O.



## SECTION – B

Answer **all** questions. Each questions carries **15** marks.

II.

- (A) (a) Describe the general formulation of time independent perturbation theory.  
(b) Discuss the non-degenerate energy levels of an harmonic oscillator.

OR

- (B) (a) Discuss the ground state energy of He atom using perturbation theory.  
(b) Using the variation method discuss the ground state and Excited state of helium atom.

III.

- (A) (a) Describe the partial wave analysis for finding scattering cross section.  
(b) Discuss the optical theorem in scattering amplitude.

OR

- (B) (a) Describe the vector function of identical particle and discuss it for two electron system.  
(b) What is central field approximation and explain Thomas Fermi model of an atom.

IV.

- (A) (a) Develop the Klein Gordon Eqn.  
(b) Find the expression for probability density, using Klein-Gordon Eqn.

OR

- (B) (a) Describe the Langrangian and Hamiltonian formulation of classical fields.  
(b) Write the concept of quantisation of fields.

**(3 × 15 = 45 Marks)**



SECTION – C

Answer **any three**. Each carries **5** marks

V. (a) Prove  $a^+ \psi_n$  is an eigen function with an eigen value  $n + 1$ .

(b) Deduce the relation

$L^2 \psi_{lm} = \hbar^2 l(l + 1) \psi_{lm}$ . Where  $\hat{L}$  total angular moments operate  $\psi_{lm}$  an wave function.

(c) Prove the Lamb shift  $\Delta E_{lam} = \frac{4}{3} \frac{mc^2 z^4 \alpha^5}{n^3} \lg \frac{1}{\alpha z} \delta_{l,0}$ .

(d) Prove that the differential the scattering  $\frac{d\sigma}{d\Omega} = |f_k(\theta, \phi)|^2$   $f(\theta, \phi)$  is the amplitude function.

(e) Prove  $\alpha_x^2 = \sigma_y^2 = \sigma_z^2 = 1$  where  $\alpha_x, \alpha_y$  and  $\alpha_z$  are Pauli's spin matrices.

(f) Develop the Dirac matrices from Pauli's spin matrix

$$r^0, r^1, r^2 \text{ and } r^3$$

Show that  $r^1, r^2$  and  $r^3$  are anti Hermitian  $r^+ = -r$

**(3 × 5 = 15 Marks)**

